

Chapter 6 Contours

Def. 6.1 Edge list; ordered set of edge points

Def. 6.2 Contour; edge list or the curve that has been used to represent the edge list

Def. 6.3 Boundary; closed contour that surrounds a region

6.1 Geometry of curves

6.2 Digital curves

digitized pixels; difficult to compute slope and curvature precisely

6.8.4 Hough transform

* Fitting a straight line

$$y = mx + c$$

$$\Rightarrow c = y - mx$$

in polar coord. to avoid singularity

$$\rho = x \cos \theta + y \sin \theta$$

$$\rho > 0$$

Algorithm 6.4 Hough transform algorithm

(1) Standard (basic) form (SHT)

(2) Polarized form (PHT)

(3) Weighted polarized form (WPHT)

* Fitting a circle

$$(x-a)^2 + (y-b)^2 = r^2$$

$$\begin{aligned}x &= a + r \cos \theta \\y &= b + r \sin \theta\end{aligned}$$

$$\begin{aligned}a &= x - r \cos \theta \\b &= y - r \sin \theta\end{aligned}$$

=>

$$b = a \tan \theta - x \tan \theta + y$$

Algorithm 6.5 Circle fitting algorithm

1. Quantize the parameter space for the a and b
2. Zero the accumulator array $M(a,b)$
3. Compute the Gradient magnitude $G(x,y)$ and angle $\theta(x,y)$
4. For each edge point in $G(x,y)$, increment all points in the accumulator array $M(a,b)$ along the line

$$b = a \tan \theta - x \tan \theta + y$$

5. Local maxima in the accumulator array correspond to centers of the circles in the image